

**DPP**  
**VECTOR**

1. If  $\vec{a}$  and  $\vec{b}$  are P.V. of two points A, B, and C divides AB in ratio 2 : 1, then P.V. of C is

- (a)  $\frac{a+2b}{3}$  (b)  $\frac{2a+b}{3}$   
(c)  $\frac{a+2}{3}$  (d)  $\frac{a+b}{2}$

2. The position vectors of two points A and B are  $\vec{i} + \vec{j} - \vec{k}$  and  $2\vec{i} - \vec{j} + \vec{k}$  respectively.

Then  $|\overrightarrow{AB}| =$

- (a) 2 (b) 3 (c) 4 (d) 5

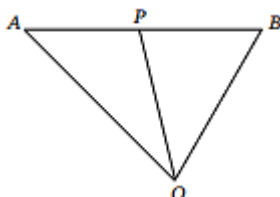
3. The position vector of the points which divides internally in the ratio 2 : 3 the join of the points  $2\vec{a} - 3\vec{b}$  and  $3\vec{a} - 2\vec{b}$ , is

- (a)  $\frac{12}{5}\vec{a} + \frac{13}{5}\vec{b}$  (b)  $\frac{12}{5}\vec{a} - \frac{13}{5}\vec{b}$   
(c)  $\frac{3}{5}\vec{a} - \frac{2}{5}\vec{b}$  (d) None of these

4. If  $\vec{a}, \vec{b}, \vec{c}$  are the position vectors of the vertices A, B, C of the triangle ABC, then the centroid of  $\Delta ABC$  is

- (a)  $\frac{a+b+c}{3}$  (b)  $\frac{1}{2}\left(a + \frac{b+c}{2}\right)$   
(c)  $a + \frac{b+c}{2}$  (d)  $\frac{a+b+c}{2}$

5. If in the given figure  $\overrightarrow{OA} = \vec{a}$ ,  $\overrightarrow{OB} = \vec{b}$  and  $AP : PB = m : n$ , then  $\overrightarrow{OP} =$



- (a)  $\frac{ma+nb}{m+n}$  (b)  $\frac{na+mb}{m+n}$   
(c)  $ma-nb$  (d)  $\frac{ma-nb}{m-n}$

6. The position vectors of A and B are  $\vec{i} - \vec{j} + 2\vec{k}$  and  $3\vec{i} - \vec{j} + 3\vec{k}$ . The position vector of the middle point of the line AB is

- (a)  $\frac{1}{2}\vec{i} - \frac{1}{2}\vec{j} + \vec{k}$  (b)  $2\vec{i} - \vec{j} + \frac{5}{2}\vec{k}$   
(c)  $\frac{3}{2}\vec{i} - \frac{1}{2}\vec{j} + \frac{3}{2}\vec{k}$  (d) None of these

7. If the position vectors of the points A and B are  $\vec{i} + 3\vec{j} - \vec{k}$  and  $3\vec{i} - \vec{j} - 3\vec{k}$ , then what

will be the position vector of the mid point of AB

- (a)  $\vec{i} + 2\vec{j} - \vec{k}$  (b)  $2\vec{i} + \vec{j} - 2\vec{k}$   
(c)  $2\vec{i} + \vec{j} - \vec{k}$  (d)  $\vec{i} + \vec{j} - 2\vec{k}$

8. A, B, C, D, E are five coplanar points, then  $\overrightarrow{DA} + \overrightarrow{DB} + \overrightarrow{DC} + \overrightarrow{AE} + \overrightarrow{BE} + \overrightarrow{CE}$  is equal to

- (a)  $\overrightarrow{DE}$  (b)  $3\overrightarrow{DE}$  (c)  $2\overrightarrow{DE}$  (d)  $4\overrightarrow{ED}$

9. If  $\vec{a} \neq \vec{0}, \vec{b} \neq \vec{0}$  and  $|\vec{a} + \vec{b}| = |\vec{a} - \vec{b}|$ , then the vectors  $\vec{a}$  and  $\vec{b}$  are

- (a) Parallel to each other  
(b) Perpendicular to each other  
(c) Inclined at an angle of  $60^\circ$   
(d) Neither perpendicular nor

10. If ABCDEF is a regular hexagon and  $\overrightarrow{AB} + \overrightarrow{AC} + \overrightarrow{AD} + \overrightarrow{AE} + \overrightarrow{AF} = \lambda \overrightarrow{AD}$ , then  $\lambda =$

- (a) 2 (b) 3 (c) 4 (d) 6

11. If O be the circumcentre and O' be the orthocentre of a triangle ABC, then

$\overrightarrow{OA} + \overrightarrow{OB} + \overrightarrow{OC} =$

- (a)  $2\overrightarrow{OO'}$  (b)  $2\overrightarrow{O'O}$   
(c)  $\overrightarrow{OO'}$  (d)  $\overrightarrow{O'O}$

12. Let  $\vec{a} = \vec{i}$  be a vector which makes an angle of  $120^\circ$  with a unit vector  $\vec{b}$ . Then the unit vector  $(\vec{a} + \vec{b})$  is

- (a)  $-\frac{1}{2}\vec{i} + \frac{\sqrt{3}}{2}\vec{j}$  (b)  $-\frac{\sqrt{3}}{2}\vec{i} + \frac{1}{2}\vec{j}$   
(c)  $\frac{1}{2}\vec{i} + \frac{\sqrt{3}}{2}\vec{j}$  (d)  $\frac{\sqrt{3}}{2}\vec{i} - \frac{1}{2}\vec{j}$

13. If  $\theta$  be the angle between the unit vectors  $\vec{a}$  and  $\vec{b}$ , then  $\cos \frac{\theta}{2} =$

- (a)  $\frac{1}{2}|\vec{a} - \vec{b}|$  (b)  $\frac{1}{2}|\vec{a} + \vec{b}|$   
(c)  $\frac{a-b}{a+b}$  (d)  $\frac{a+b}{a-b}$

14. If  $|\vec{a}| = 3, |\vec{b}| = 4, |\vec{c}| = 5$  and  $\vec{a} + \vec{b} + \vec{c} = \vec{0}$ , then the angle between  $\vec{a}$  and  $\vec{b}$  is

- (a) 0 (b)  $\frac{\pi}{6}$  (c)  $\frac{\pi}{3}$  (d)  $\frac{\pi}{2}$

15. If ABCD is a parallelogram,  $\overrightarrow{AB} = 2i + 4j - 5k$  and  $\overrightarrow{AD} = i + 2j + 3k$ , then the unit vector in the direction of  $BD$  is

- (a)  $\frac{1}{\sqrt{69}}(i+2j-8k)$  (b)  $\frac{1}{69}(i+2j-8k)$   
 (c)  $\frac{1}{\sqrt{69}}(-i-2j+8k)$  (d)  $\frac{1}{69}(-i-2j+8k)$

16. If  $a$  and  $b$  are unit vectors making an angle  $\theta$  with each other then  $|a - b|$

- (a) 1 (b) 0 (c)  $\cos \frac{\theta}{2}$  (d)  $2\sin \frac{\theta}{2}$

17. If the moduli of the vectors  $a, b, c$  are 3, 4, 5 respectively and  $a$  and  $b + c, b$  and  $c + a, c$  and  $a + b$  are mutually perpendicular, then the modulus of  $a + b + c$  is

- (a)  $\sqrt{12}$  (b) 12 (c)  $5\sqrt{2}$  (d) 50

18. If  $a$  and  $b$  are unit vectors and  $a - b$  is also a unit vector, then the angle between  $a$  and  $b$  is

- (a)  $\frac{\pi}{4}$  (b)  $\frac{\pi}{3}$  (c)  $\frac{\pi}{2}$  (d)  $\frac{2\pi}{3}$

19. If  $a = 3i - 2j + k, b = 2i - 4j - 3k$  and  $c = -i + 2j + 2k$ , then  $a + b + c$  is

- (a)  $3i - 4j$  (b)  $3i + 4j$   
 (c)  $4i - 4j$  (d)  $4i + 4j$

20. If  $x$  and  $y$  are two unit vectors and  $\pi$  is the angle between them, then  $|x - y|$  is equal to

- (a) 0 (b)  $\pi/2$  (c) 1 (d)  $\pi/4$

21. If  $D, E, F$  are respectively the mid points of  $AB, AC$  and  $BC$  in  $\Delta ABC$ , then

$\overrightarrow{BE} + \overrightarrow{AF} =$

- (a)  $\overrightarrow{DC}$  (b)  $\frac{1}{2}\overrightarrow{BF}$  (c)  $2\overrightarrow{BF}$  (d)  $\frac{3}{2}\overrightarrow{BF}$

22. If ABCD is a rhombus whose diagonals cut at the origin  $O$ , then  $\overrightarrow{OA} + \overrightarrow{OB} + \overrightarrow{OC} + \overrightarrow{OD}$  equals

- (a)  $\overrightarrow{AB} + \overrightarrow{AC}$  (b)  $\vec{O}$   
 (c)  $2(\overrightarrow{AB} + \overrightarrow{BC})$  (d)  $\overrightarrow{AC} + \overrightarrow{BD}$

23. ABCD is a parallelogram with  $AC$  and  $BD$  as diagonals. Then  $\overrightarrow{AC} - \overrightarrow{BD} =$

- (a)  $4\overrightarrow{AB}$  (b)  $3\overrightarrow{AB}$  (c)  $2\overrightarrow{AB}$  (d)  $\overrightarrow{AB}$

24. The vectors  $b$  and  $c$  are in the direction of north-east and north-west respectively and  $|b| = |c| = 4$ . The magnitude and direction of the vector  $d = c - b$ , are

- (a)  $4\sqrt{2}$ , towards north (b)  $4\sqrt{2}$ , towards west  
 (c) 4, towards east (d) 4, towards south

25. Let  $a$  and  $b$  be two unit vectors inclined at an angle  $\theta$ , then  $\sin(\theta/2)$  is equal to

- (a)  $\frac{1}{2}|a - b|$  (b)  $\frac{1}{2}|a + b|$   
 (c)  $|a - b|$  (d)  $|a + b|$

26. If  $a, b, c$  are three vectors such that  $a = b + c$  and the angle between  $b$  and  $c$  is  $\pi/2$ , then

- (a)  $a^2 = b^2 + c^2$  (b)  $b^2 = c^2 + a^2$   
 (c)  $c^2 = a^2 + b^2$  (d)  $2a^2 = b^2 + c^2$

(Note : Here  $a = |a|, b = |b|, c = |c|$ )

27. If the sum of two unit vectors is a unit vector, then the angle between them is equal to

- (a)  $\frac{\pi}{6}$  (b)  $\frac{\pi}{3}$  (c)  $\frac{\pi}{2}$  (d)  $\frac{2\pi}{3}$

28. If  $|a| = 3, |b| = 4$  and  $|a + b| = 5$ , then  $|a - b| =$

- (a) 6 (b) 5 (c) 4 (d) 3

29. In the triangle  $ABC, \overrightarrow{AB} = a, \overrightarrow{AC} = c, \overrightarrow{BC} = b$ , then

- (a)  $a + b + c = 0$  (b)  $a + b - c = 0$   
 (c)  $a - b + c = 0$  (d)  $-a + b + c = 0$

30. If  $p = 7i - 2j + 3k$  and  $q = 3i + j + 5k$ , then the magnitude of  $p - 2q$  is

- (a)  $\sqrt{29}$  (b) 4  
 (c)  $\sqrt{62} - 2\sqrt{35}$  (d)  $\sqrt{66}$

31. If  $C$  is the middle point of  $AB$  and  $P$  is any point outside  $AB$ , then

- (a)  $\overrightarrow{PA} + \overrightarrow{PB} = \overrightarrow{PC}$   
 (b)  $\overrightarrow{PA} + \overrightarrow{PB} = 2\overrightarrow{PC}$   
 (c)  $\overrightarrow{PA} + \overrightarrow{PB} + \overrightarrow{PC} = 0$   
 (d)  $\overrightarrow{PA} + \overrightarrow{PB} + 2\overrightarrow{PC} = 0$

32. If  $a = 2i + 5j$  and  $b = 2i - j$ , then the unit vector along  $a + b$  will be

- (a)  $\frac{i-j}{\sqrt{2}}$  (b)  $i + j$   
 (c)  $\sqrt{2}(i + j)$  (d)  $\frac{i-j}{\sqrt{2}}$

33. What should be added in vector  $a = 3i + 4j - 2k$  to get its resultant a unit vector  $i$

- (a)  $-2i - 4j + 2k$  (b)  $-2i + 4j - 2k$   
 (c)  $2i + 4j - 2k$  (d) None of these

34. If  $a = i + 2j + 3k$ ,  $b = -i + 2j + k$  and  $c = 3i + j$ , then the unit vector along its resultant is

- (a)  $3i + 5j + 4k$  (b)  $\frac{3i+5j+4k}{50}$   
 (c)  $\frac{3i+5j+4k}{5\sqrt{2}}$  (d) None of these

35. P is the point of intersection of the diagonals of the parallelogram ABCD. If O is any point, then  $\vec{OA} + \vec{OB} + \vec{OC} + \vec{OD} =$

- (a)  $\vec{OP}$  (b)  $2\vec{OP}$  (c)  $3\vec{OP}$  (d)  $4\vec{OP}$

36. The perimeter of a triangle with sides  $3i + 4j + 5k$ ,  $4i - 3j - 5k$  and  $7i + j$  is

- (a)  $\sqrt{450}$  (b)  $\sqrt{150}$   
 (c)  $\sqrt{50}$  (d)  $\sqrt{200}$

37. The magnitudes of mutually perpendicular forces  $a$ ,  $b$  and  $c$  are 2, 10 and 11 respectively. Then the magnitude of its resultant is

- (a) 12 (b) 15 (c) 9 (d) None of these

38. If  $a = 2i + j - 8k$  and  $b = i + 3j - 4k$ , then the magnitude of  $a + b =$

- (a) 13 (b)  $\frac{13}{3}$  (c)  $\frac{3}{13}$  (d)  $\frac{4}{13}$

39. The position vectors of A and B are  $2i - 9j - 4k$ , and  $6i - 3j + 8k$  respectively, then the magnitude of AB is

- (a) 11 (b) 12 (c) 13 (d) 14

40. If the position vectors of P and Q are  $(i + 3j - 7k)$  and  $(5i - 2j + 4k)$ , then  $|\vec{PQ}|$  is

- (a)  $\sqrt{158}$  (b)  $\sqrt{160}$   
 (c)  $\sqrt{161}$  (d)  $\sqrt{162}$

41. If  $a$ ,  $b$ ,  $c$  are mutually perpendicular unit vectors, then  $|a + b + c| =$

- (a)  $\sqrt{3}$  (b) 3 (c) 1 (d) 0

42. Let  $a = i + j + pk$  and  $b = i + j + k$ , then  $|a + b| = |a| + |b|$ , holds for

- (a) All real  $p$  (b) No real  $p$   
 (c)  $p = -1$  (d)  $p = 1$

43. For any two vectors  $a$  and  $b$ , which of the following is true

- (a)  $|a + b| \geq |a| + |b|$   
 (b)  $|a + b| = |a| + |b|$   
 (c)  $|a + b| < |a| + |b|$   
 (d)  $|a + b| \leq |a| + |b|$

44. If  $a$  and  $b$  are the adjacent sides of a parallelogram, then  $|a + b| = |a - b|$  is a necessary and sufficient condition for the parallelogram to be a

- (a) Rhombus (b) Square  
 (c) Rectangle (d) Trapezium

45. The direction cosines of vector  $a = 3i + 4j + 5k$  in the direction of positive axis of  $x$ , is

- (a)  $\pm \frac{3}{\sqrt{50}}$  (b)  $\frac{4}{\sqrt{50}}$   
 (c)  $\frac{3}{\sqrt{50}}$  (d)  $-\frac{4}{\sqrt{50}}$

46. A force is a

- (a) Unit vector (b) Localised vector  
 (c) Zero vector (d) Free vector

47. A zero vector has

- (a) Any direction (b) No direction  
 (c) Many directions (d) None of these

48. The position vectors of two points A and B are  $i + j - k$  and  $2i - j + k$  respectively.

Then  $|AB| =$

- (a) 2 (b) 3 (c) 4 (d) 5

49. The position vector of the points which divides internally in the ratio 2 : 3 the join of the points  $2a - 3b$  and  $3a - 2b$ , is

- (a)  $\frac{12}{5}a + \frac{13}{5}b$  (b)  $\frac{12}{5}a - \frac{13}{5}b$   
 (c)  $\frac{3}{5}a - \frac{2}{5}b$  (d) None of these

50. If  $a$  and  $b$  are P.V. of two points A, B, and C divides AB in ratio 2 : 1, then P.V. of C is

- (a)  $\frac{a+2b}{3}$  (b)  $\frac{2a+b}{3}$   
 (c)  $\frac{a+2}{3}$  (d)  $\frac{a+b}{2}$

51. If three points A, B, C whose position vector are respectively  $i - 2j - 8k$ ,  $5i - 2k$  and  $11i + 3j + 7k$  are collinear, then the ratio in which B divides AC is

- (a) 1 : 2 (b) 2 : 3 (c) 2 : 1 (d) 1 : 1

52. If O is the origin and C is the mid point of A (2, -1) and B (-4, 3). Then value of  $\overrightarrow{OC}$  is

- (a)  $i + j$  (b)  $i - j$  (c)  $-i + j$  (d)  $-i - j$

53. If the position vectors of P and Q are  $i + 3j - 7k$  and  $5i - 2j + 4k$  respectively, then  $\overrightarrow{PQ}$  is equal to

- (a)  $-4i + 5j - 11k$  (b)  $4i - 5j + 11k$   
 (c)  $i + j + k$  (d) None of these

54. The position vectors of two vertices and the centroid of a triangle are  $i + j$ ,  $2i - j + k$  and  $k$  respectively. The position vector of the third vertex of the triangle is

- (a)  $-3i + 2k$  (b)  $3i - 2k$   
 (c)  $i + 3j + 2k$  (d) None of these

55. The position vector of three consecutive vertices of a parallelogram are  $i + j + k$ ,  $i + 3j + 5k$  and  $7i + 9j + 11k$  respectively. The position vector of the fourth vertex is

- (a)  $7(i + j + k)$  (b)  $5(i + j + k)$   
 (c)  $6i + 8j + 10k$  (d) None of these

54. If  $a$  and  $b$  are two non-zero vectors, then the component of  $b$  along  $a$  is

- (a)  $\frac{(a \cdot b)a}{b \cdot b}$  (b)  $\frac{(a \cdot b)b}{a \cdot a}$  (c)  $\frac{(a \cdot b)b}{a \cdot b}$  (d)  $\frac{(a \cdot b)a}{a \cdot a}$

55. Projection of the vector  $i - 2j + k$  in the direction of the vector  $4i - 4j + 7k$  will be

- (a)  $\frac{5\sqrt{6}}{10}$  (b)  $\frac{9}{19}$  (c)  $\frac{19}{9}$  (d)  $\frac{\sqrt{6}}{19}$

56. If  $a = 4i + 6j$  and  $b = 3j + 4k$ , then the component of  $a$  along  $b$  is

- (a)  $\frac{18}{10\sqrt{3}}(3j + 4k)$  (b)  $\frac{18}{25}(3j + 4k)$   
 (c)  $\frac{18}{\sqrt{3}}(3j + 4k)$  (d)  $(3j + 4k)$

57. The projection of vector  $2i + 3j - 2k$  on the vector  $i + 2j + 3k$  will be

- (a)  $\frac{1}{\sqrt{14}}$  (b)  $\frac{2}{\sqrt{14}}$  (c)  $\frac{3}{\sqrt{14}}$  (d)  $\sqrt{14}$

58. If vector  $a = 2i - 3j + 6k$  and vector  $b = -2i + 2j - k$ , then

Projection of vector  $a$  on vector  $b$  =  
 Projection of vector  $b$  on vector  $a$

- (a)  $\frac{3}{7}$  (b)  $\frac{7}{3}$  (c) 3 (d) 7

59. The projection of  $a$  along  $b$  is

- (a)  $\frac{a \cdot b}{|a|}$  (b)  $\frac{a \times b}{|a|}$  (c)  $\frac{a \cdot b}{|b|}$  (d)  $\frac{a \times b}{|b|}$

60. If  $a = 2i + j + 2k$  and  $b = 5i - 3j + k$ , then the projection of  $b$  on  $a$  is

- (a) 3 (b) 4 (c) 5 (d) 6

61. The projection of the vector  $i + j + k$  along the vector  $j$  is

- (a) 1 (b) 0 (c) 2 (d) -1

62. If  $\hat{a}$  is a unit vector and  $b$ , a non-zero vector not parallel to  $\hat{a}$ , then the vector  $b - (\hat{a} \cdot b)\hat{a}$  is

- (a) Parallel to  $b$  (b) At right angles to  $\hat{a}$   
 (c) Parallel to  $\hat{a}$  (d) At right angles to  $b$

63. The angle between the vectors  $2i + 3j + k$  and  $2i - j - k$  is

- (a) 0 (b)  $\frac{\pi}{4}$  (c)  $\frac{\pi}{6}$  (d)  $\frac{\pi}{2}$

64. If  $a = 2i + 2j + 3k$ ,  $b = -i + 2j + k$  and  $c = 3i + j$ , then  $a + tb$  is perpendicular to  $c$  if  $t =$

- (a) 2 (b) 4 (c) 6 (d) 8

65. The angle between the vectors  $3i + j + 2k$  and  $2i - 2j + 4k$  is

- (a)  $\cos^{-1} \frac{2}{\sqrt{7}}$  (b)  $\sin^{-1} \frac{2}{\sqrt{7}}$   
 (c)  $\cos^{-1} \frac{2}{\sqrt{5}}$  (d)  $\sin^{-1} \frac{2}{\sqrt{5}}$

66. If  $a, b, c$  are non zero-vectors such that  $a \cdot b = a \cdot c$ , then which statement is true

- (a)  $b = c$  (b)  $a \perp (b - c)$   
(c)  $b = c$  or  $a \perp (b - c)$  (d) None of these

67. The vector  $2i + aj + k$  is perpendicular to the vector  $2i - j - k$ , if  $a =$

- (a) 5 (b) -5 (c) -3 (d) 3

68. The vector  $2i + j - k$  is perpendicular to the vector  $i - 4j + \lambda k$ , if  $\lambda =$

- (a) 0 (b) -1 (c) -2 (d) -3

69. If the vectors  $ai - 2j + 3k$  and  $3i + 6j - 5k$  are perpendicular to each other, then  $a$  is given by

- (a) 9 (b) 16 (c) 25 (d) 36

70. The value of  $\lambda$  for which the vectors  $2\lambda i + j - k$  and  $2j + k$  are perpendicular, is

- (a) None (b) -1 (c) 1 (d) Any

71. The angle between the vectors  $i - j + k$  and  $i + 2j + k$  is

- (a)  $\cos^{-1}\left(\frac{1}{\sqrt{15}}\right)$  (b)  $\cos^{-1}\left(\frac{4}{\sqrt{15}}\right)$   
(c)  $\cos^{-1}\left(\frac{4}{\sqrt{15}}\right)$  (d)  $\frac{\pi}{2}$

72. If  $\lambda$  is a unit vector perpendicular to plane of vector  $a$  and  $b$  and angle between them is  $\theta$ , then  $a \cdot b$  will be

- (a)  $|a| |b| \sin\theta \vec{\lambda}$  (b)  $|a| |b| \cos\theta \vec{\lambda}$   
(c)  $|a| |b| \cos\theta$  (d)  $|a| |b| \sin\theta$

73. If the vectors  $ai + bj + ck$  and  $pi + qj + rk$  are perpendicular, then

- (a)  $(a + b + c)(p + q + r) = 0$   
(b)  $(a + b + c)(p + q + r) = 1$   
(c)  $ap + bq + cr = 0$   
(d)  $ap + bq + cr = 1$

74. If  $\theta$  be the angle between two vectors  $a$  and  $b$ , then  $a \cdot b \geq 0$  if

- (a)  $0 \leq \theta \leq \pi$  (b)  $\frac{\pi}{2} \leq \theta \leq \pi$   
(c)  $0 \leq \theta \leq \frac{\pi}{2}$  (d) None of these

75. If  $a = 2i + 4j + 2k$  and  $b = 8i - 3j + \lambda k$  and  $a \perp b$ , then value of  $\lambda$  will be

- (a) 2 (b) -1 (c) -2 (d) 1

76. If  $a$  and  $b$  are mutually perpendicular vectors, then  $(a + b)^2$

- (a)  $a + b$  (b)  $a - b$   
(c)  $a^2 - b^2$  (d)  $(a - b)^2$

77. If  $a = i + 2j - 3k$  and  $b = 3i - j + 2k$ , then the angle between the vectors  $a + b$  and  $a - b$  is

- (a)  $30^\circ$  (b)  $60^\circ$  (c)  $90^\circ$  (d) 0

78.  $a \cdot b = 0$ , then

- (a)  $a \perp b$   
(b)  $a \parallel b$   
(c) Angle between  $a$  and  $b$  is  $60^\circ$   
(d) None of these

79. The angle between the vectors

$(2i + 6j + 3k)$  and  $(12i - 4j + 3k)$  is

- (a)  $\cos^{-1}\left(\frac{1}{10}\right)$  (b)  $\cos^{-1}\left(\frac{9}{11}\right)$   
(c)  $\cos^{-1}\left(\frac{9}{91}\right)$  (d)  $\cos^{-1}\left(\frac{1}{9}\right)$

80. If the vectors  $ai + 2j + 3k$  and  $-i + 5j + ak$  are perpendicular to each other, then  $a =$

- (a) 6 (b) -6 (c) 5 (d) -5

81. If the angle between two vectors  $i + k$  and  $i - j + ak$  is  $\pi/3$ , then the value of  $a =$

- (a) 2 (b) 4 (c) -2 (d) 0

82.  $(a \cdot b)c$  and  $(a \cdot c)b$  are

- (a) Two like vectors  
(b) Two equal vectors  
(c) Two vectors in direction of  $a$   
(d) None of these

83. The angle between the vector  $2i + 3j + k$  and  $2i - j - k$  is

- (a)  $\frac{\pi}{2}$  (b)  $\frac{\pi}{4}$  (c)  $\frac{\pi}{3}$  (d) 0

84. If  $a = (1, -1, 2)$ ,  $b = (-2, 3, 5)$ ,  $c = (2, -2, 4)$  and  $i$  is the unit vector in the x-direction, then  $(a - 2b + 3c) \cdot i =$

- (a) 11 (b) 15 (c) 18 (d) 36

**85. If  $a\mathbf{i} + 6\mathbf{j} - \mathbf{k}$  and  $7\mathbf{i} - 3\mathbf{j} + 17\mathbf{k}$  are perpendicular vectors, then the value of  $a$  is**

- (a) 5 (b)  $-5$  (c) 7 (d)  $\frac{1}{7}$

**86. If  $\mathbf{a} + \mathbf{b} \perp \mathbf{a}$  and  $|\mathbf{b}| = \sqrt{2} |\mathbf{a}|$  then**

- (a)  $(2\mathbf{a} + \mathbf{b}) \parallel \mathbf{b}$  (b)  $(2\mathbf{a} + \mathbf{b}) \perp \mathbf{b}$   
(c)  $(2\mathbf{a} - \mathbf{b}) \perp \mathbf{b}$  (d)  $(2\mathbf{a} + \mathbf{b}) \perp \mathbf{a}$

**87. If  $\mathbf{a}$  and  $\mathbf{b}$  are adjacent sides of a rhombus, then**

- (a)  $\mathbf{a} \cdot \mathbf{b} = 0$  (b)  $\mathbf{a} \times \mathbf{b} = 0$   
(c)  $\mathbf{a} \cdot \mathbf{a} = \mathbf{b} \cdot \mathbf{b}$  (d) None of these

**88. If  $|\mathbf{a}| = |\mathbf{b}|$ , then  $(\mathbf{a} + \mathbf{b}) \cdot (\mathbf{a} - \mathbf{b})$  is**

- (a) Positive (b) Negative  
(c) Zero (d) None of these

**89. If  $4\mathbf{i} + \mathbf{j} - \mathbf{k}$  and  $3\mathbf{i} + m\mathbf{j} + 2\mathbf{k}$  are at right angle, then  $m =$**

- (a)  $-6$  (b)  $-8$  (c)  $-10$  (d)  $-12$

**90. If the vectors  $3\mathbf{i} + \lambda\mathbf{j} + \mathbf{k}$  and  $2\mathbf{i} - \mathbf{j} + 8\mathbf{k}$  are perpendicular, then  $\lambda$  is**

- (a)  $-14$  (b) 7 (c) 14 (d)  $\frac{1}{7}$

**91.  $(\mathbf{a} \cdot \mathbf{i})^2 + (\mathbf{a} \cdot \mathbf{j})^2 + (\mathbf{a} \cdot \mathbf{k})^2$  is equal to**

- (a)  $a^2$  (b) 3  
(c)  $|\mathbf{a} \cdot (\mathbf{i} + \mathbf{j} + \mathbf{k})|^2$  (d) None of these

**92. If the vectors  $\mathbf{i} - 2\mathbf{x}\mathbf{j} - 3\mathbf{y}\mathbf{k}$  and  $\mathbf{i} + 3\mathbf{x}\mathbf{j} + 2\mathbf{y}\mathbf{k}$  are orthogonal to each other, then the locus of the point  $(x, y)$  is**

- (a) A circle (b) An ellipse  
(c) A parabola (d) A straight line

**93. If  $\vec{A} = \mathbf{i} + 2\mathbf{j} + 3\mathbf{k}$ ,  $\vec{B} = -\mathbf{i} + 2\mathbf{j} + \mathbf{k}$  and  $\vec{C} = 3\mathbf{i} + \mathbf{j}$ , then the value of  $t$  such that  $\mathbf{A} + t\mathbf{B}$  is at right angle to vector  $\mathbf{C}$ , is**

- (a) 3 (b) 4 (c) 5 (d) 6

**94. If  $\mathbf{a}$  and  $\mathbf{b}$  are two perpendicular vectors, then out of the following four statements**

- (i)  $(\mathbf{a} + \mathbf{b})^2 = (\mathbf{a})^2 + (\mathbf{b})^2$   
(ii)  $(\mathbf{a} - \mathbf{b})^2 = (\mathbf{a})^2 + (\mathbf{b})^2$

(iii)  $|\mathbf{a} + \mathbf{b}|^2 = |\mathbf{a}|^2 + |\mathbf{b}|^2$

(iv)  $(\mathbf{a} + \mathbf{b})^2 = (\mathbf{a} - \mathbf{b})^2$

- (a) Only one is correct  
(b) Only two are correct  
(c) Only three are correct  
(d) All the four are correct

**95. If  $\mathbf{a} = \mathbf{i} - 2\mathbf{j}$  and  $\mathbf{b} = 2\mathbf{i} + \lambda\mathbf{j}$  are parallel, then  $\lambda$  is**

- (a) 4 (b) 2 (c)  $-2$  (d)  $-4$

**96. The vectors  $3\mathbf{i} + \mathbf{j} - 5\mathbf{k}$  and  $a\mathbf{i} + b\mathbf{j} - 15\mathbf{k}$  are collinear, if**

- (a)  $a = 3, b = 1$  (b)  $a = 9, b = 1$   
(c)  $a = 3, b = 3$  (d)  $a = 9, b = 3$

**97. If  $\mathbf{a} = (1, -1)$  and  $\mathbf{b} = (-2, m)$  are two collinear vectors, then  $m =$**

- (a) 4 (b) 3 (c) 2 (d) 0

**98. If  $\mathbf{a}, \mathbf{b}, \mathbf{c}$  are the position vectors of three collinear points, then the existence of  $x, y, z$  is such that**

- (a)  $x\mathbf{a} + y\mathbf{b} + z\mathbf{c} = 0, x + y + z \neq 0$   
(b)  $x\mathbf{a} + y\mathbf{b} + z\mathbf{c} \neq 0, x + y + z = 0$   
(c)  $x\mathbf{a} + y\mathbf{b} + z\mathbf{c} \neq 0, x + y + z \neq 0$   
(d)  $x\mathbf{a} + y\mathbf{b} + z\mathbf{c} = 0, x + y + z = 0$

**99. If  $\mathbf{a}$  and  $\mathbf{b}$  are two non-collinear vectors, then  $x\mathbf{a} + y\mathbf{b} = 0$**

- (a)  $x = 0$ , but  $y$  is not necessarily zero  
(b)  $y = 0$ , but  $x$  is not necessarily zero  
(c)  $x = 0, y = 0$   
(d) None of these

**100. If  $\mathbf{a}$  and  $\mathbf{b}$  are two non-collinear vectors, then  $x\mathbf{a} + y\mathbf{b}$  (where  $x$  and  $y$  are scalars) represents a vector which is**

- (a) Parallel to  $\mathbf{b}$   
(b) Parallel to  $\mathbf{a}$   
(c) Coplanar with  $\mathbf{a}$  and  $\mathbf{b}$   
(d) None of these

**101. If  $\mathbf{a}, \mathbf{b}, \mathbf{c}$  are non-collinear vectors such that for some scalars  $x, y, z, x\mathbf{a} + y\mathbf{b} + z\mathbf{c} = 0$ , then**

- (a)  $x = 0, y = 0, z = 0$       (b)  $x \neq 0, y \neq 0, z = 0$   
 (c)  $x = 0, y \neq 0, z \neq 0$       (d)  $x \neq 0, y \neq 0, z \neq 0$

**102.** If the position vectors of the points A, B, C be  $\mathbf{a}, \mathbf{b}, 3\mathbf{a} - 2\mathbf{b}$  respectively, then the points A, B, C are

- (a) Collinear  
 (b) Non-collinear  
 (c) Form a right angled triangle  
 (d) None of these

**103.** If two vertices of a triangle are  $\mathbf{i} - \mathbf{j}$  and  $\mathbf{j} + \mathbf{k}$ , then the third vertex can be

- (a)  $\mathbf{i} + \mathbf{k}$                       (b)  $\mathbf{i} - 2\mathbf{j} - \mathbf{k}$   
 (c)  $\mathbf{i} - \mathbf{k}$                       (d)  $2\mathbf{i} - \mathbf{j}$

**104.** If the vectors  $3\mathbf{i} + 2\mathbf{j} - \mathbf{k}$  and  $6\mathbf{i} - 4\mathbf{j} + \mathbf{k}$  are parallel, then the value of  $x$  and  $y$  will be

- (a)  $-1, -2$                       (b)  $1, -2$   
 (c)  $-1, 2$                         (d)  $1, 2$

**104.** The position vectors of four points P, Q, R, S are  $2\mathbf{a} + 4\mathbf{c}, 5\mathbf{a} + 3\sqrt{3}\mathbf{b} + 4\mathbf{c}, -2\sqrt{3}\mathbf{b} + \mathbf{c}$  and  $2\mathbf{a} + \mathbf{c}$  respectively, then

- (a) PQ is parallel to RS  
 (b) PQ is not parallel to RS  
 (c) PQ is equal to RS  
 (d) PQ is parallel and equal to RS

**105.** The vectors  $2\mathbf{i} + 3\mathbf{j}, 5\mathbf{i} + 6\mathbf{j}$  and  $8\mathbf{i} + \lambda\mathbf{j}$  have their initial points at  $(1, 1)$ . The value of  $\lambda$  so that the vectors terminate on one straight line, is

- (a) 0      (b) 3                      (c) 6      (d) 9

**106.** The points with position vectors  $20\mathbf{i} + \mathbf{p}\mathbf{j}, 5\mathbf{i} - \mathbf{j}$  and  $10\mathbf{i} - 13\mathbf{j}$  are collinear. The value of  $\mathbf{p}$  is

- (a) 7      (b)  $-37$                       (c)  $-7$                       (d) 3

### Advance

**107.** The point B divides the arc AC of a quadrant of a circle in the ratio  $1 : 2$ . If O is the centre and  $\overrightarrow{OA} = \mathbf{a}$  and  $\overrightarrow{OB} = \mathbf{b}$ , then the vector  $\overrightarrow{OC}$  is

- (a)  $\mathbf{b} - 2\mathbf{a}$                       (b)  $2\mathbf{a} - \mathbf{b}$

- (c)  $3\mathbf{b} - 2\mathbf{a}$                       (d) None of these

**108.** The point having position vectors  $2\mathbf{i} + 3\mathbf{j} + 4\mathbf{k}, 3\mathbf{i} + 4\mathbf{j} + 2\mathbf{k}, 4\mathbf{i} + 2\mathbf{j} + 3\mathbf{k}$  are the vertices of

- (a) Right angled triangle  
 (b) Isosceles triangle  
 (c) Equilateral triangle  
 (d) Collinear

**109.** Let  $\mathbf{p}$  and  $\mathbf{q}$  be the position vectors of P and Q respectively with respect to O and  $|\mathbf{p}| = p, |\mathbf{q}| = q$ . The points R and S divide PQ internally and externally in the ratio  $2 : 3$  respectively. If  $\overrightarrow{OR}$  and  $\overrightarrow{OS}$  are perpendicular, then

- (a)  $9p^2 = 4q^2$                       (b)  $4p^2 = 9q^2$   
 (c)  $9p = 4q$                         (d)  $4p = 9q$

**110.** The position vectors of the points A, B, C are  $(2\mathbf{i} + \mathbf{j} - \mathbf{k}), (3\mathbf{i} - 2\mathbf{j} + \mathbf{k})$  and  $(\mathbf{i} + 4\mathbf{j} - 3\mathbf{k})$  respectively. These points

- (a) Form an isosceles triangle  
 (b) Form a right-angled triangle  
 (c) Are collinear  
 (d) Form a scalene triangle

**111.** ABCDEF is a regular hexagon where centre O is the origin. If the position vectors of A and B are  $\mathbf{i} - \mathbf{j} + 2\mathbf{k}$  and  $2\mathbf{i} + \mathbf{j} - \mathbf{k}$  respectively, then  $\overrightarrow{BC}$  is equal to

- (a)  $\mathbf{i} - \mathbf{j} + 2\mathbf{k}$                       (b)  $-\mathbf{i} + \mathbf{j} - 2\mathbf{k}$   
 (c)  $3\mathbf{i} + 3\mathbf{j} - 4\mathbf{k}$                       (d) None of these

**112.** Let  $\overrightarrow{AB} = 3\mathbf{i} + \mathbf{j} - \mathbf{k}$  and  $\overrightarrow{AC} = \mathbf{i} - \mathbf{j} + 3\mathbf{k}$ . If the point P on the line segment BC is equidistant from AB and AC, then  $\overrightarrow{AP}$  is

- (a)  $2\mathbf{i} - \mathbf{k}$                         (b)  $\mathbf{i} - 2\mathbf{k}$   
 (c)  $2\mathbf{i} + \mathbf{k}$                         (d) None of these

**113.** If  $4\mathbf{i} + 7\mathbf{j} + 8\mathbf{k}, 2\mathbf{i} + 3\mathbf{j} + 4\mathbf{k},$  and  $2\mathbf{i} + 5\mathbf{j} + 7\mathbf{k}$  are the position vectors of the vertices A, B and C respectively of triangle ABC. The position vector of the point where the bisector of angle A meets BC, is

- (a)  $\frac{2}{3}(-6\mathbf{i} - 8\mathbf{j} - 6\mathbf{k})$                       (b)  $\frac{2}{3}(6\mathbf{i} + 8\mathbf{j} + 6\mathbf{k})$

(c)  $\frac{1}{3}(6i + 13j + 18k)$       (d)  $\frac{1}{3}(5j + 12k)$

114. If  $a$  and  $b$  are the position vectors of  $A$  and  $B$  respectively, then the position vector of a point  $C$  on  $AB$  produced such that  $\overrightarrow{AC} = 3\overrightarrow{AB}$  is

- (a)  $3a - b$                       (b)  $3b - a$   
(c)  $3a - 2b$                       (d)  $3b - 2a$

115. If the position vectors of the points  $A, B, C, D$  be  $2i + 3j + 5k, i + 2j + 3k, -5i + 4j - 2k$  and  $i + 10j + 10k$  respectively, then

- (a)  $\overrightarrow{AB} = \overrightarrow{CD}$                       (b)  $\overrightarrow{AB} \parallel \overrightarrow{CD}$   
(c)  $\overrightarrow{AB} \perp \overrightarrow{CD}$                       (d) None of these

116. The position vector of a point  $C$  with respect to  $B$  is  $i + j$  and that of  $B$  with respect to  $A$  is  $i - j$ . The position vector of  $C$  with respect to  $A$  is

- (a)  $2i$       (b)  $2j$       (c)  $-2j$       (d)  $-2i$

117.  $A$  and  $B$  are two points. The position vector of  $A$  is  $6b - 2a$ . A point  $P$  divides the line  $AB$  in the ratio  $1 : 2$ . If  $a - b$  is the position vector of  $P$ , then the position vector of  $B$  is given by

- (a)  $7a - 15b$                       (b)  $7a + 15b$   
(c)  $15a - 7b$                       (d)  $15a + 7b$

118. The points  $D, E, F$  divide  $BC, CA$  and  $AB$  of the triangle  $ABC$  in the ratio  $1 : 4, 3 : 2$  and  $3 : 7$  respectively and the point  $K$  divides  $AB$  in the ratio  $1 : 3$ , then  $(\overrightarrow{AD} + \overrightarrow{BE} + \overrightarrow{CF}) : \overrightarrow{CK}$  is equal to

- (a)  $1 : 1$                               (b)  $2 : 5$   
(c)  $5 : 2$                               (d) None of these

119. Three points whose position vectors are  $a, b, c$  will be collinear if

- (a)  $\lambda a + \mu b = (\lambda + \mu)c$   
(b)  $a \times b + b \times c + c \times a = 0$   
(c)  $[a \ b \ c] = 0$   
(d) None of these

120. If  $p = i - 2j + 3k$  and  $q = 3i + j + 2k$ , then a vector along  $r$  which is linear combination of  $p$  and  $q$  and also perpendicular to  $q$  is

- (a)  $i + 5j - 4k$                       (b)  $i - 5j + 4k$   
(c)  $-\frac{1}{2}(i + 5j - 4k)$                       (d) None of these

121. If  $a$  and  $b$  are two non zero and non-collinear vectors, then  $a + b$  and  $a - b$  are

- (a) Linearly dependent vectors  
(b) Linearly independent vectors  
(c) Linearly dependent and independent vectors  
(d) None of these

122. If  $p, q$  are two non-collinear and non-zero vectors such that  $(b - c)p \times q + (c - a)p + (a - b)q = 0$ , where  $a, b, c$  are the lengths of the sides of a triangle, then the triangle is

- (a) Right angled                      (b) Obtuse angled  
(c) Equilateral                      (d) Isosceles

123. If  $r = 3i + 2j - 5k, a = 2i - j + k, b = i + 3j - 2k$  and  $c = -2i + j - 3k$  such that  $r = \lambda a + \mu b + \nu c$  then

- (a)  $\mu, \frac{\lambda}{2}, \nu$  are in A.P.                      (b)  $\lambda, \mu, \nu$  are in A.P.  
(c)  $\lambda, \mu, \nu$  are in H.P.                      (d)  $\mu, \lambda, \nu$  are in G.P.

124. Let  $a, b, c$  are three non-coplanar vectors such that  $r_1 = a - b + c, r_2 = b + c - a, r_3 = c + a + b, r = 2a - 3b + 4c$ . If  $r = \lambda_1 r_1 + \lambda_2 r_2 + \lambda_3 r_3$ , then

- (a)  $\lambda_1 = 7$                               (b)  $\lambda_1 + \lambda_3 = 3$   
(c)  $\lambda_1 + \lambda_2 + \lambda_3 = 4$                       (d)  $\lambda_3 + \lambda_2 = 2$

125. If  $c = 2a - 3b$  and  $2c = 3a + 4b$  then  $c$  and  $a$  are

- (a) Like parallel vectors  
(b) Unlike parallel vectors  
(c) Are at right angles  
(d) None of these

126. The sides of a triangle are in A.P., then the line joining the centroid to the incentre is parallel to

- (a) The largest side                      (b) The smaller side  
(c) The middle side                      (d) None of the sides



127. In a trapezoid the vector  $\overrightarrow{BC} = \lambda \overrightarrow{AD}$ . We will then find that  $p = \overrightarrow{AC} + \overrightarrow{BD}$  is collinear with AD. If  $p = \mu \overrightarrow{AD}$ , then

- (a)  $\mu = \lambda + 1$                       (b)  $\lambda = \mu + 1$   
 (c)  $\lambda + \mu = 1$                       (d)  $\mu = 2 + \lambda$

128. If the vectors  $6i - 2j + 3k$ ,  $2i + 3j - 6k$  and  $3i + 6j - 2k$  form a triangle, then it is

- (a) Right angled                      (b) Obtuse angled  
 (c) Equilateral                      (d) Isosceles

129. The vectors  $\overrightarrow{AB} = 3i + 4k$  and  $\overrightarrow{AC} = 5i - 2j + 4k$  are the sides of a triangle ABC. The length of the median through A is

- (a)  $\sqrt{18}$                       (b)  $\sqrt{72}$   
 (c)  $\sqrt{33}$                       (d)  $\sqrt{288}$

130. If a and b are two unit vectors inclined at an angle  $2\theta$  to each other, then  $|a + b| < 1$ , if

- (a)  $\frac{\pi}{3} < \theta < \frac{2\pi}{3}$                       (b)  $\theta < \frac{\pi}{3}$   
 (c)  $\theta < \frac{2\pi}{3}$                       (d)  $\theta = \frac{\pi}{2}$

131. If the position vectors of A and B are  $i + 3j - 7k$  and  $5i - 2j + 4k$ , then the direction cosine of AB along y-axis is [MNR 1989]

- (a)  $\frac{4}{\sqrt{162}}$                       (b)  $-\frac{5}{\sqrt{162}}$                       (c) -5                      (d) 11

132. The position vectors of four points A, B, C, D lying in plane are a, b, c, d respectively. They satisfy the relation  $|a - d| = |b - d| = |c - d|$ , then the point D is

- (a) Centroid of  $\Delta ABC$   
 (b) Circumcentre of  $\Delta ABC$   
 (c) Orthocentre of  $\Delta ABC$   
 (d) Incentre of  $\Delta ABC$

133. In a parallelopiped the ratio of the sum of the squares on the four diagonals to the sum of the squares on the three coterminous edges is

- (a) 2                      (b) 3                      (c) 4                      (d) 1

134. The perimeter of the triangle whose vertices have the position vectors  $(i + j + k)$ ,  $(5i + 3j - 3k)$  and  $(2i + 5j + 9k)$  is given by

- (a)  $15 + \sqrt{157}$                       (b)  $15 - \sqrt{157}$   
 (c)  $\sqrt{15} - \sqrt{157}$                       (d)  $\sqrt{15} + \sqrt{157}$

135. The horizontal force and the force inclined at an angle  $60^\circ$  with the vertical, whose resultant is in vertical direction of P kg, are [IIT 1983]

- (a) P, 2P                      (b) P,  $P\sqrt{3}$   
 (c) 2P,  $P\sqrt{3}$                       (d) None of these

136. If the resultant of two forces is of magnitude P and equal to one of them and perpendicular to it, then the other force is

- (a)  $P\sqrt{2}$                       (b) P  
 (c)  $P\sqrt{3}$                       (d) None of these

137. ABC is an isosceles triangle right angled at A. Forces of magnitude  $2\sqrt{2}$ , 5 and 6 act along  $\overrightarrow{BC}$ ,  $\overrightarrow{CA}$  and  $\overrightarrow{AB}$  respectively. The magnitude of their resultant force is

- (a) 4                      (b) 5                      (c)  $11 + 2\sqrt{2}$                       (d) 30

138. If the resultant of two forces of magnitudes P and Q acting at a point at an angle of  $60^\circ$  is  $\sqrt{7}Q$ , then P / Q is

- (a) 1                      (b) 3/2                      (c) 2                      (d) 4

139. Five points given by A, B, C, D, E are in a plane. Three forces  $\overrightarrow{AC}$ ,  $\overrightarrow{AD}$  and  $\overrightarrow{AE}$  act at A and three forces  $\overrightarrow{CB}$ ,  $\overrightarrow{DB}$ ,  $\overrightarrow{EB}$  act at B. Then their resultant is

- (a)  $2\overrightarrow{AC}$                       (b)  $3\overrightarrow{AB}$                       (c)  $3\overrightarrow{DB}$                       (d)  $2\overrightarrow{BC}$

140. A point O is the centre of a circle circumscribed about a triangle ABC. Then  $\overrightarrow{OA} \sin 2A + \overrightarrow{OB} \sin 2B + \overrightarrow{OC} \sin 2C$  is equal to

- (a)  $(\overrightarrow{OA} + \overrightarrow{OB} + \overrightarrow{OC}) \sin 2A$   
 (b)  $3 \cdot \overrightarrow{OG}$ , where G is the centroid of triangle ABC  
 (c)  $\vec{O}$   
 (d) None of these

141. If  $a + b + c = \alpha d$ ,  $b + c + d = \beta a$  and  $a, b, c$  are non-coplanar, then the sum of  $a + b + c + d =$

- (a) 0  
 (b)  $(\beta - 1)d + (\alpha - 1)a$   
 (c)  $(\alpha - 1)d - (\beta - 1)a$   
 (d)  $(\alpha - 1)d + (\beta - 1)a$

142. Let  $a$  and  $b$  be two non-parallel unit vectors in a plane. If the vectors  $(\alpha a + b)$  bisects the internal angle between  $a$  and  $b$ , then  $\alpha$  is

- (a)  $\frac{1}{2}$  (b) 1 (c) 2 (d) 4

143. If  $a, b, c$  are three vectors of equal magnitude and the angle between each pair of vectors is  $\frac{\pi}{3}$  such that  $|a + b + c| = \sqrt{6}$  then  $|a|$  is equal to

- (a) 2 (b) -1 (c) 1 (d)  $\frac{1}{3}\sqrt{6}$

144. Let  $a, b, c$  be three unit vectors such that  $|a + b + c| = 1$  and  $a \perp b$ . If  $c$  makes angles  $\alpha, \beta$  with  $a, b$  respectively then  $\cos \alpha + \cos \beta$  is equal to

- (a)  $\frac{3}{2}$  (b) 1 (c) -1 (d) None of these

145. A vector of magnitude 2 along a bisector of the angle between the two vectors  $2i - 2j + k$  and  $i + 2j - 2k$  is

- (a)  $\frac{3}{\sqrt{10}}(3i - k)$  (b)  $\frac{3}{\sqrt{26}}(i - 4j + 3k)$   
 (c)  $\frac{2}{\sqrt{26}}(i - 4j + 3k)$  (d) None of these

146. The vector  $i + xj + 3k$  is rotated through an angle  $\theta$  and doubled in magnitude, then it becomes  $4i + (4x - 2)j + 2k$ . The value of  $x$  is

- (a)  $-\frac{2}{3}$  (b)  $\frac{1}{3}$  (c)  $\frac{2}{3}$  (d) 2

147. If  $I$  is the centre of a circle inscribed in a triangle  $ABC$ , then  $|\vec{BC}| + |\vec{IA}| + |\vec{CA}| + |\vec{IB}| + |\vec{AB}| + |\vec{IC}|$  is

- (a) 0 (b)  $|\vec{IA}| + |\vec{IB}| + |\vec{IC}|$   
 (c)  $\frac{|\vec{IA}| + |\vec{IB}| + |\vec{IC}|}{3}$  (d) None of these

148. If the vector  $-i + j - k$  bisects the angle between the vector  $e$  and the vector  $3i + 4j$ , then the unit vector in the direction of  $e$  is

- (a)  $\frac{1}{15}(11i + 10j + 2k)$  (b)  $-\frac{1}{15}(11i - 10j + 2k)$   
 (c)  $-\frac{1}{15}(11i + 10j - 2k)$  (d)  $-\frac{1}{15}(11i + 10j + 2k)$

149. The sides of a parallelogram are  $2i + 4j - 5k, i + 2j + 3k$ , then the unit vector parallel to one of the diagonals

- (a)  $\frac{1}{7}(3i + 6j - 2k)$  (b)  $\frac{1}{7}(3i - 6j - 2k)$   
 (c)  $\frac{1}{7}(-3i + 6j - 2k)$  (d)  $\frac{1}{7}(3i + 6j + 2k)$

150. If  $p, q$  are two non-collinear and non-zero vectors such that  $(b - c)p \times q + (c - a)p + (a - b)q = 0$ , where  $a, b, c$  are the lengths of the sides of a triangle, then the triangle is

- (a) Right angled (b) Obtuse angled  
 (c) Equilateral (d) Isosceles

151. If  $r = 3i + 2j - 5k, a = 2i - j + k, b = i + 3j - 2k$  and  $c = -2i + j - 3k$  such that  $r = \lambda a + \mu b + \nu c$  then

- (a)  $\lambda, \mu, \nu$  are in A.P.  
 (b)  $\lambda, \mu, \nu$  are in A.P.  
 (c)  $\lambda, \mu, \nu$  are in H.P.  
 (d)  $\mu, \lambda, \nu$  are in G.P.

152. Let  $a, b, c$  are three non-coplanar vectors such that  $r_1 = a - b + c, r_2 = b + c - a, r_3 = c + a + b, r = 2a - 3b + 4c$ . If  $r = \lambda_1 r_1 + \lambda_2 r_2 + \lambda_3 r_3$ , then

- (a)  $\lambda_1 = 7$  (b)  $\lambda_1 + \lambda_3 = 3$   
 (c)  $\lambda_1 + \lambda_2 + \lambda_3 = 4$  (d)  $\lambda_3 + \lambda_2 = 2$

153. If  $c = 2a - 3b$  and  $2c = 3a + 4b$  then  $c$  and  $a$  are

- (a) Like parallel vectors  
 (b) Unlike parallel vectors  
 (c) Are at right angles  
 (d) None of these

154. The sides of a triangle are in A.P., then the line joining the centroid to the incentre is parallel to

- (a) The largest side (b) The smaller side  
 (c) The middle side (d) None of the sides

155. In a trapezoid the vector  $\overrightarrow{BC} = \lambda \overrightarrow{AD}$ . We will then find that  $\mathbf{p} = \overrightarrow{AC} + \overrightarrow{BD}$  is collinear with AD. If  $\mathbf{p} = \mu \overrightarrow{AD}$ , then

- (a)  $\mu = \lambda + 1$                       (b)  $\lambda = \mu + 1$   
 (c)  $\lambda + \mu = 1$                       (d)  $\mu = 2 + \lambda$

156. Three points whose position vectors are  $\mathbf{a} + \mathbf{b}$ ,  $\mathbf{a} - \mathbf{b}$  and  $\mathbf{a} + k\mathbf{b}$  will be collinear, if the value of  $k$  is

- (a) Zero  
 (b) Only negative real number  
 (c) Only positive real number  
 (d) Every real number

157. The points with position vectors  $10\mathbf{i} + 3\mathbf{j}$ ,  $12\mathbf{i} - 5\mathbf{j}$  and  $a\mathbf{i} + 11\mathbf{j}$  are collinear, if  $a =$

- (a) -8      (b) 4      (c) 8      (d) 12

158. Let the value of  $\mathbf{p} = (x + 4\mathbf{y})\mathbf{a} + (2x + \mathbf{y} + 1)\mathbf{b}$  and  $\mathbf{q} = (\mathbf{y} - 2x + 2)\mathbf{a} + (2x - 3\mathbf{y} - 1)\mathbf{b}$ , where  $\mathbf{a}$  and  $\mathbf{b}$  are non-collinear vectors. If  $3\mathbf{p} = 2\mathbf{q}$ , then the value of  $x$  and  $y$  will be

- (a) -1, 2                      (b) 2, -1  
 (c) 1, 2                      (d) 2, 1

159. If  $(x, y, z) \neq (0, 0, 0)$  and  $(\mathbf{i} + \mathbf{j} + 3\mathbf{k})x + (3\mathbf{i} - 3\mathbf{j} + \mathbf{k})y + (-4\mathbf{i} + 5\mathbf{j})z = \lambda(x\mathbf{i} + y\mathbf{j} + z\mathbf{k})$ , then the value of  $\lambda$  will be

- (a) -2, 0      (b) 0, -2      (c) -1, 0      (d) 0, -1

160. The vectors  $\mathbf{i} + 2\mathbf{j} + 3\mathbf{k}$ ,  $\lambda\mathbf{i} + 4\mathbf{j} + 7\mathbf{k}$ ,  $-3\mathbf{i} - 2\mathbf{j} - 5\mathbf{k}$  are collinear, if  $\lambda$  equals

- (a) 3      (b) 4      (c) 5      (d) 6

161. If three points A, B and C have position vectors  $(1, x, 3)$ ,  $(3, 4, 7)$  and  $(y, -2, -5)$  respectively and if they are collinear, then  $(x, y) =$

- (a) (2, -3)                      (b) (-2, 3)  
 (c) (2, 3)                      (d) (-2, -3)

162. The position vectors of three points are  $2\mathbf{a} - \mathbf{b} + 3\mathbf{c}$ ,  $\mathbf{a} - 2\mathbf{b} + \lambda\mathbf{c}$  and  $\mu\mathbf{a} - 5\mathbf{b}$  where  $\mathbf{a}$ ,  $\mathbf{b}$ ,  $\mathbf{c}$  are non-coplanar vectors. The points are collinear when

- (a)  $\lambda = -2, \mu = \frac{9}{4}$                       (b)  $\lambda = -\frac{9}{4}, \mu = 2$   
 (c)  $\lambda = \frac{9}{4}, \mu = -2$                       (d) None of these

163. Three points whose position vectors are  $\mathbf{a}$ ,  $\mathbf{b}$ ,  $\mathbf{c}$  will be collinear if

- (a)  $\lambda\mathbf{a} + \mu\mathbf{b} = (\lambda + \mu)\mathbf{c}$   
 (b)  $\mathbf{a} \times \mathbf{b} + \mathbf{b} \times \mathbf{c} + \mathbf{c} \times \mathbf{a} = 0$   
 (c)  $[\mathbf{a} \ \mathbf{b} \ \mathbf{c}] = 0$   
 (d) None of these

164. If  $\mathbf{p} = \mathbf{i} - 2\mathbf{j} + 3\mathbf{k}$  and  $\mathbf{q} = 3\mathbf{i} + \mathbf{j} + 2\mathbf{k}$ , then a vector along  $\mathbf{r}$  which is linear combination of  $\mathbf{p}$  and  $\mathbf{q}$  and also perpendicular to  $\mathbf{q}$  is

- (a)  $\mathbf{i} + 5\mathbf{j} - 4\mathbf{k}$                       (b)  $\mathbf{i} - 5\mathbf{j} + 4\mathbf{k}$   
 (c)  $-\frac{1}{2}(\mathbf{i} + 5\mathbf{j} - 4\mathbf{k})$                       (d) None of these

165. If  $\mathbf{a}$  and  $\mathbf{b}$  are two non zero and non-collinear vectors, then  $\mathbf{a} + \mathbf{b}$  and  $\mathbf{a} - \mathbf{b}$  are

- (a) Linearly dependent vectors  
 (b) Linearly independent vectors  
 (c) Linearly dependent and independent vectors  
 (d) None of these

166. If  $\mathbf{a} = \mathbf{i} + 2\mathbf{j} + 2\mathbf{k}$  and  $\mathbf{b} = 3\mathbf{i} + 6\mathbf{j} + 2\mathbf{k}$ , then a vector in the direction of  $\mathbf{a}$  and having magnitude as  $|\mathbf{b}|$  is

- (a)  $7(\mathbf{i} + \mathbf{j} + \mathbf{k})$                       (b)  $\frac{7}{3}(\mathbf{i} + 2\mathbf{j} + 2\mathbf{k})$   
 (c)  $\frac{7}{9}(\mathbf{i} + \mathbf{j} + \mathbf{k})$                       (d) None of these

167. The vector  $\mathbf{b} = 3\mathbf{j} + 4\mathbf{k}$  is to be written as the sum of a vector  $\mathbf{b}_1$  parallel to  $\mathbf{a} = \mathbf{i} + \mathbf{j}$  and a vector  $\mathbf{b}_2$  perpendicular to  $\mathbf{a}$ . Then  $\mathbf{b}_1 =$

- (a)  $\frac{3}{2}(\mathbf{i} + \mathbf{j})$                       (b)  $\frac{2}{3}(\mathbf{i} + \mathbf{j})$   
 (c)  $\frac{1}{2}(\mathbf{i} + \mathbf{j})$                       (d)  $\frac{1}{3}(\mathbf{i} + \mathbf{j})$

168. The components of a vector  $\mathbf{a}$  along and perpendicular to the non-zero vector  $\mathbf{b}$  are respectively

- (a)  $\frac{\mathbf{a} \cdot \mathbf{b}}{|\mathbf{a}|}, \frac{\mathbf{a} \times \mathbf{b}}{|\mathbf{a}|}$                       (b)  $\frac{\mathbf{a} \cdot \mathbf{b}}{|\mathbf{b}|}, \frac{\mathbf{a} \times \mathbf{b}}{|\mathbf{b}|}$   
 (c)  $\frac{\mathbf{a} \cdot \mathbf{b}}{|\mathbf{a}|}, \frac{\mathbf{a} \cdot \mathbf{b}}{|\mathbf{a}|}$                       (d)  $\frac{\mathbf{a} \times \mathbf{b}}{|\mathbf{a}|}, \frac{\mathbf{a} \times \mathbf{b}}{|\mathbf{b}|}$

169. The value of  $x$  for which the angle between the vectors  $\mathbf{a} = x\mathbf{i} - 3\mathbf{j} - \mathbf{k}$  and  $\mathbf{b} = 2x\mathbf{i}$

$+xj - k$  is acute and the angle between the vector  $b$  and  $y$ -axis lies between  $\frac{\pi}{2}$  and  $\pi$  are  
 (a)  $< 0$  (b)  $> 0$  (c)  $-2, -3$  (d)  $1, 2$

170. If  $a, b, c$  are linearly independent vectors

and  $\Delta = \begin{vmatrix} a & b & c \\ a \cdot a & a \cdot b & a \cdot c \\ a \cdot c & b \cdot c & c \cdot c \end{vmatrix}$ , then

- (a)  $\Delta = 0$   
 (b)  $\Delta = 1$   
 (c)  $\Delta =$  any non-zero value  
 (d) None of these

171. The position vectors of the points A, B and C are  $i + j + k, i + 5j - k$  and  $2i + 3j + 5k$  respectively. The greatest angle of the triangle ABC is

- (a)  $135^\circ$  (b)  $90^\circ$   
 (c)  $\cos^{-1}\left(\frac{2}{3}\right)$  (d)  $\cos^{-1}\left(\frac{5}{7}\right)$

172.  $a, b, c$  are three vectors, such that  $a + b + c = 0, |a| = 1, |b| = 2, |c| = 3$ , then  $a \cdot b + b \cdot c + c \cdot a$  is equal to

- (a) 0 (b)  $-7$  (c) 7 (d) 1

173. A unit vector in  $xy$ -plane that makes an angle  $45^\circ$  with the vectors  $(i + j)$  and an angle of  $60^\circ$  with the vector  $(3i - 4j)$  is

- (a)  $i$  (b)  $\frac{1}{\sqrt{2}}(i - j)$   
 (c)  $\frac{1}{\sqrt{2}}(i + j)$  (d) None of these

174. The angle between the vectors  $a + b$  and  $a - b$ , when  $a = (1, 1, 4)$  and  $b = (1, -1, 4)$  is  
 (a)  $90^\circ$  (b)  $45^\circ$  (c)  $30^\circ$  (d)  $15^\circ$

175. Let  $u = i + j, v = i - j$  and  $w = i + 2j + 3k$ . If  $n$  is a unit vector such that  $u \cdot n = 0$  and  $v \cdot n = 0$ , then  $|w \cdot n|$  is equal to  
 (a) 0 (b) 1 (c) 2 (d) 3

176. If  $a, b, c$  are the  $p$ th,  $q$ th,  $r$ th terms of an HP and  $u = (q - r)i + (r - p)j + (p - q)k, v = \frac{i}{a} + \frac{j}{b} + \frac{k}{c}$ , then

- (a)  $u, v$  are parallel vectors  
 (b)  $u, v$  are orthogonal vectors

- (c)  $u \cdot v = 1$   
 (d)  $u \times v = i + j + k$

177. The value of  $x$  for which the angle between the vectors  $a = -3i + xj + k$  and  $b = xi + 2xj + k$  is acute and the angle between  $b$  and  $x$ -axis lies between  $\frac{\pi}{2}$  and  $\pi$  satisfy

- (a)  $x > 0$  (b)  $x < 0$   
 (c)  $x > 1$  only (d)  $x < -1$  only

178. If the scalar product of the vector  $i + j + k$  with a unit vector parallel to the sum of the vectors  $2i + 4j - 5k$  and  $\lambda i + 2j + 3k$  be 1, then  $\lambda =$

- (a) 1 (b)  $-1$  (c) 2 (d)  $-2$

179. If  $a$  is any vector in space, then

- (a)  $a = (a \cdot i)i + (a \cdot j)j + (a \cdot k)k$   
 (b)  $a = (a \times i) + (a \times j) + (a \times k)$   
 (c)  $a = j(a \cdot i) + k(a \cdot j) + i(a \cdot k)$   
 (d)  $a = (a \times i) \times i + (a \times j) \times j + (a \times k) \times k$

180. If  $a, b$  and  $c$  are unit vectors, then  $|a - b|^2 + |b - c|^2 + |c - a|^2$  does not exceed  
 (a) 4 (b) 9 (c) 8 (d) 6

181. If  $a$  and  $b$  are two unit vectors, such that  $a + 2b$  and  $5a - 4b$  are perpendicular to each other then the angle between  $a$  and  $b$  is  
 (a)  $45^\circ$  (b)  $60^\circ$   
 (c)  $\cos^{-1}\left(\frac{1}{3}\right)$  (d)  $\cos^{-1}\left(\frac{2}{7}\right)$

182. The position vector of coplanar points A, B, C, D are  $a, b, c$  and  $d$  respectively, in such a way that  $(a - d) \cdot (b - c) = (b - d) \cdot (c - a) = 0$ , then the point D of the triangle ABC is  
 (a) Incentre (b) Circumcentre  
 (c) Orthocentre (d) None of these

183. If  $\vec{F}_1 = i - j + k, \vec{F}_2 = -i + 2j - k, \vec{F}_3 = j - k, A = 4i - 3j - 2k$  and  $B = 6i + j - 3k$ , then the scalar product of  $F_1 + F_2 + F_3$  and  $AB$  will be  
 (a) 3 (b) 6 (c) 9 (d) 12

184. If the moduli of  $a$  and  $b$  are equal and angle between them is  $120^\circ$  and  $a \cdot b = -8$ , then  $|a|$  is equal to

- (a)  $-5$  (b)  $-4$  (c)  $4$  (d)  $5$

185. The position vector of vertices of a triangle ABC are  $4i - 2j$ ,  $i + 4j - 3k$  and  $-i + 5j + k$  respectively, then  $\angle ABC =$

- (a)  $\frac{\pi}{6}$  (b)  $\frac{\pi}{4}$  (c)  $\frac{\pi}{3}$  (d)  $\frac{\pi}{2}$

186. A, B, C, D are any four points, then  $\overrightarrow{AB} \cdot \overrightarrow{CD} + \overrightarrow{BC} \cdot \overrightarrow{AD} + \overrightarrow{CA} \cdot \overrightarrow{BD} =$

- (a)  $2\overrightarrow{AB} \cdot \overrightarrow{BC} \cdot \overrightarrow{CD}$  (b)  $\overrightarrow{AB} + \overrightarrow{BC} + \overrightarrow{CD}$   
(c)  $5\sqrt{3}$  (d)  $0$

187. If  $|a| = 3, |b| = 1, |c| = 4$  and  $a + b + c = 0$ , then  $a \cdot b + b \cdot c + c \cdot a =$

- (a)  $-13$  (b)  $-10$  (c)  $13$  (d)  $10$

188. The value of  $c$  so that for all real  $x$ , the vectors  $cx\mathbf{i} - 6\mathbf{j} + 3\mathbf{k}$ ,  $x\mathbf{i} + 2\mathbf{j} + 2cx\mathbf{k}$  make an obtuse angle are

- (a)  $c < 0$  (b)  $0 < c < \frac{3}{4}$   
(c)  $-\frac{3}{4} < c < 0$  (d)  $c > 0$

189. The vector  $\frac{1}{3}(2\mathbf{i} - 2\mathbf{j} + \mathbf{k})$  is

- (a) A unit vector  
(b) Makes an angle  $\frac{\pi}{3}$  with the vector  $2\mathbf{i} - 4\mathbf{j} + 3\mathbf{k}$   
(c) Parallel to the vector  $-\mathbf{i} + \mathbf{j} - \frac{1}{2}\mathbf{k}$   
(d) Perpendicular to the vector  $3\mathbf{i} + 2\mathbf{j} - 2\mathbf{k}$

190. If  $a, b, c$  are unit vectors such that  $a + b + c = 0$ , then  $a \cdot b + b \cdot c + c \cdot a =$

- (a)  $1$  (b)  $3$  (c)  $-\frac{3}{2}$  (d)  $\frac{3}{2}$

191. A unit vector in the  $xy$ -plane which is perpendicular to  $4\mathbf{i} - 3\mathbf{j} + \mathbf{k}$  is

- (a)  $\frac{\mathbf{i} + \mathbf{j}}{\sqrt{2}}$  (b)  $\frac{1}{5}(3\mathbf{i} + 4\mathbf{j})$   
(c)  $\frac{1}{5}(3\mathbf{i} - 4\mathbf{j})$  (d) None of these

192. The vectors  $2\mathbf{i} + 3\mathbf{j} - 4\mathbf{k}$  and  $a\mathbf{i} + b\mathbf{j} + c\mathbf{k}$  are perpendicular, when

- (a)  $a = 2, b = 3, c = -4$  (b)  $a = 4, b = 4, c = 5$   
(c)  $a = 4, b = 4, c = -5$  (d) None of these

193. The unit normal vector to the line joining  $\mathbf{i} - \mathbf{j}$  and  $2\mathbf{i} + 3\mathbf{j}$  and pointing towards the origin is

- (a)  $\frac{4\mathbf{i} - \mathbf{j}}{\sqrt{17}}$  (b)  $\frac{-4\mathbf{i} - \mathbf{j}}{\sqrt{17}}$  (c)  $\frac{2\mathbf{i} - 3\mathbf{j}}{\sqrt{13}}$  (d)  $\frac{-2\mathbf{i} + 3\mathbf{j}}{\sqrt{13}}$

## ANSWERS

1	a	41	d	81	d	121	b	161	a
2	b	42	d	82	d	122	c	162	c
3	b	43	c	83	d	123	a	163	b
4	a	44	c	84	a	124	b	164	a
5	b	45	b	85	a	125	a	165	b
6	b	46	a	86	a	126	c	166	b
7	b	47	b	87	b	127	a	167	a
8	b	48	b	88	c	128	b	168	b
9	b	49	a	89	c	129	c	169	a
10	b	50	b	90	c	130	a	170	c
11	c	51	c	91	c	131	b	171	b
12	b	52	b	92	a	132	b	172	b
13	d	53	a	93	a	133	c	173	d
14	c	54	a	94	c	134	a	174	a
15	d	55	d	95	d	135	c	175	d
16	c	56	c	96	d	136	a	176	b
17	b	57	b	97	d	137	b	177	b
18	c	58	b	98	c	138	c	178	a
19	c	59	b	99	d	139	b	179	a
20	a	60	c	100	c	140	c	180	b
21	c	61	a	101	c	141	a	181	b
22	c	62	a	102	a	142	b	182	c
23	b	63	b	103	a	143	c	183	c
24	a	64	d	104	a,b,c	144	c	184	c
25	a	65	d	105	a	145	a,c	185	d
26	d	66	b	106	a	146	a,d	186	d
27	b	67	c	107	d	147	a	187	a
28	b	68	d	108	b	148	d	188	c
29	d	69	c	109	c	149	a	189	a,c,d
30	b	70	a	110	c	150	c	190	c
31	d	71	a	111	a	151	a	191	b
32	a	72	d	112	c	152	b	192	b
33	c	73	c	113	b	153	a	193	b
34	d	74	c	114	c	154	c		
35	a	75	c	115	c	155	a		
36	b	76	c	116	d	156	d		
37	a	77	d	117	b	157	c		
38	d	78	c	118	a	158	b		
39	d	79	a	119	a	159	d		
40	a	80	c	120	b	160	a		